

#### Grade 8: New Jersey Student Learning Standards for Mathematics - Prerequisite Standards and Learning Objectives by Domain

#### Description

Included here are the prerequisite concepts and skills necessary for students to learn grade level content based on the New Jersey Student Learning Standards in mathematics. This tool is intended to support educators in the identification of any gaps in conceptual understanding or skill that might exist in a student's understanding of mathematics standards. The organization of this document mirrors that of the New Jersey Student Learning Standards for mathematics, includes all grade- or course-level standards and the associated student learning objectives, and reflects a grouping of the standards by domain.

The tables are divided into three columns. The first column contains the grade level standard and student learning objectives, which reflect the corresponding concepts and skills in that standard. The second column contains standards from prior grades and the corresponding learning objectives, which reflect prerequisite concepts and skills essential for student attainment of the grade level standard as listed on the left. Given that a single standard may reflect multiple concepts and skills, all learning objectives for a prior grade standard may not be listed. Only those prior grade learning objectives that reflect prerequisite concepts and skills important for attainment of the associated grade level standard is listed. The third column contains the recommendations from <u>Student Achievement Partners' recommendations</u> (SAP) for the 2020-21 school year regarding preserving or reducing time as compared to a typical academic year.

Content Emphases Key: E: Major Cluster : Supporting Cluster

• Additional Cluster

**Note:** Double asterisks (\*\*) indicate that the example(s) included within the New Jersey Student Learning Standard may be especially informative when considering the Student Learning Objective.

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.NS.A.1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number</li> <li>We are learning to/that</li> <li>numbers that are not rational are called irrational</li> <li>every number has a decimal expansion</li> <li>show that rational numbers have decimal expansions that either terminate in zeros or repeats eventually</li> <li>convert a repeating decimal to a rational number</li> </ul>	<ul> <li>7.NS.A.2 Apply and extend previous understandings of multiplication and division of fractions to multiply and divide rational numbers.</li> <li>d. Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats.</li> <li>We have learned to/that</li> <li>convert a rational number to a decimal using long division.</li> </ul>	<i>Integrate</i> foundational irrational numbers with students' work on square roots (8.EE.A.2) and the Pythagorean (8.G.B.7).
<b>8.NS.A.2</b> Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., $\pi^2$ ). <i>For example</i> , by truncating the decimal expansion of $\sqrt{2}$ , show that $\sqrt{2}$ is between 1 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations.	n/a	<i>Integrate</i> foundational irrational numbers with students' work on square roots (8.EE.A.2) and the Pythagorean (8.G.B.7).

**Domain: The Number System** 

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>We are learning to/that</li> <li>estimate the value of irrational numbers using rational approximations</li> <li>use rational approximations of irrational numbers to compare their size</li> <li>use rational approximations of irrational numbers to locate them on a number line</li> </ul>		

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<ul> <li>8.EE.A.1 Know and apply the properties of integer exponents to generate equivalent numerical expressions. <i>For example</i>, 3<sup>2</sup> × 3<sup>-5</sup> = 3<sup>-3</sup> =1/3<sup>3</sup> = 1/27.</li> <li>We are learning to/that</li> <li>know the properties of integer exponents</li> <li>determine whether two numerical expressions involving integer exponents are equivalent</li> <li>generate equivalent expressions using the properties of exponents</li> </ul>	<ul> <li>6.EE.A.1. Write and evaluate numerical expressions involving whole-number exponents.</li> <li>We have learned to/that</li> <li>write a numerical expression using whole-number exponents</li> </ul>	For curricula and lessons that are well aligned to work of integer exponents as detailed by the standard, <i>no special</i> <i>considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.
<ul> <li>■ 8.EE.A.2 Use square root and cube root symbols to represent solutions to equations of the form x<sup>2</sup> = p and x<sup>3</sup> = p, where p is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that √2 is irrational.</li> <li>We are learning to/that</li> <li>use square root and cube root symbols to represent solutions to equations in the form x<sup>2</sup> = p and x<sup>3</sup> = p</li> <li>evaluate square roots of small perfect squares and cube roots of small perfect.</li> </ul>	<ul> <li>7.NS.A.3 Solve real-world and mathematical problems involving the four operations with rational numbers.</li> <li>We have learned to/that</li> <li>solve real-world and mathematical problems involving the four operations with rational numbers in decimal form</li> <li>6.EE.B.5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.</li> </ul>	<i>Eliminate</i> lessons and problems about cube roots.

# **Domain: Expressions and Equations**

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.EE.A.3 Use numbers expressed in the form of a single digit times an integer power of 10 to estimate very large or very small quantities, and to express how many times as much one is than the other. <i>For example</i>, estimate the population of the United States as 3 × 108 and the population of the world as 7 × 109, and determine that the world population is more than 20 times larger.</li> <li>We are learning to/that</li> <li>estimate a very large or very small number as a single digit times an integer power of ten</li> <li>express how many times larger one quantity is compared to another when written as a single digit times an integer power of ten</li> </ul>	<ul> <li>We have learned to/that</li> <li>determine if a given number from a specified set is a solution to an equation or an inequality using substitution</li> <li><b>5.NBT.A.2</b> Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.</li> <li>We have learned to/that</li> <li>denote powers of 10 by using whole-number exponents.</li> </ul>	<ul> <li><i>Eliminate</i> lessons and practice dedicated to calculating with scientific notation.</li> <li><i>Include</i> examples of numbers expressed in scientific notation in lessons about integer exponents as examples of how integer exponents are applicable outside of mathematics classes (8.EE.A.1)</li> <li>Note: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>
<b>8.EE.A.4</b> Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Use scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific	■ 7.EE.B.3 Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers	<i>Eliminate</i> lessons and practice dedicated to calculating with scientific notation. <i>Include</i> examples of numbers expressed in scientific notation in lessons about integer exponents as examples of how integer

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notation that has been generated by technology.	using mental computation and estimation strategies.	exponents are applicable outside of mathematics classes (8.EE.A.1).
<ul> <li>We are learning to/that</li> <li>add, subtract, multiply, and divide numbers expressed in scientific notation</li> <li>add, subtract, multiply, and divide numbers where one is expressed in decimal notation and the other is expressed in scientific notation</li> <li>choose appropriate units to represent measurements of very large or very small quantities</li> <li>interpret scientific notation generated by technology as a number multiplied by a power of ten</li> </ul>	<ul> <li>We have learned to/that</li> <li>convert between forms (fractions, decimals, and whole numbers) as appropriate to solve multi-step real life and mathematical problems with positive and negative rational numbers in any form</li> </ul>	Note: While these standards or clusters are Major Work of the Grade, during the 2020- 21 school year, it is recommended that they receive lighter treatment.
<ul> <li>8.EE.B.5 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. <i>For example</i>, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.</li> <li>We are learning to/that</li> <li>graph proportional relationships represented in different ways (i.e. ordered pairs, table, equation, phrases, etc.)</li> </ul>	<ul> <li><b>7.RP.A.2</b> Recognize and represent proportional relationships between quantities.</li> <li>a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.</li> <li>b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.</li> </ul>	For curricula and lessons that are well aligned to the work of understanding the connections between proportional relationships, lines, and linear equations as detailed by the cluster, <i>no special</i> <i>considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.

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<ul> <li>recognize that for proportional relationships, the unit rate is the slope of the graph</li> <li>compare the unit rates of two proportional relationships represented in different ways</li> </ul>	<ul> <li>We have learned to/that</li> <li>decide whether two quantities show a proportional relationship by graphing on a coordinate plane and observing whether the graph is a straight line through the origin.</li> <li>identify the constant of proportionality (unit rate) in equations and verbal descriptions of proportional relationships.</li> <li>identify the constant of proportionality (unit rate) in tables, graphs, and diagrams.</li> </ul>	
<ul> <li>8.EE.B.6 Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b.</li> <li>We are learning to/that</li> <li>explain why the slope is the same between any two distinct points on a non-vertical line by drawing similar right triangles and comparing the ratios of their sides</li> <li>derive the equation y = mx + b for a line through the origin</li> <li>derive the equation y = mx + b for a line intercepting the y-axis at b</li> </ul>	<ul> <li>7.RP.A.2 Recognize and represent proportional relationships between quantities.</li> <li>a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.</li> <li>We have learned to/that</li> <li>decide whether two quantities show a proportional relationship by testing for equivalent ratios in a table</li> </ul>	For curricula and lessons that are well aligned to the work of understanding the connections between proportional relationships, lines, and linear equations as detailed by the cluster, <i>no special</i> <i>considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.

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<ul> <li>8.EE.C.7 Solve linear equations in one variable.</li> <li>a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers).</li> <li>b. Solve linear equations with rational number coefficients, including equations</li> </ul>	<ul> <li>7.EE.A.1 Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.</li> <li>We have learned to/that</li> <li>apply the properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.</li> <li>7.EE.B.4 Use variables to represent quantities in a real-world or mathematical</li> </ul>	<i>Incorporate</i> students' work on rewriting expressions (7.EE.A) and solving algebraic equations (7.EE.B.4) to support students in analyzing and solving one-variable linear equations.
whose solutions require expanding expressions using the distributive property and collecting like terms.	<ul><li>problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.</li><li>a. Solve word problems leading to equations</li></ul>	
<ul> <li>We are learning to/that</li> <li>a linear equation in one variable can result in one solution, infinitely many solutions, or no solution</li> <li>show which of these outcomes is the case by transforming the original equation into the form x = a, a = a, or a = b</li> <li>solve linear equations in one variable with rational number coefficients, including equations that require expanding expressions using the distributive property and combining like terms</li> </ul>	<ul> <li>of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. <i>For example,</i> the perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width? We have learned to/that</li> <li>solve equations of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers with accuracy</li> </ul>	

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<ul> <li>8.EE.C.8 Analyze and solve pairs of simultaneous linear equations.</li> <li>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</li> <li>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6.</li> <li>c. Solve real-world and mathematical problems leading to two linear equations in two variables. <i>For example</i>, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.</li> </ul>	<ul> <li>6.EE.B.5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.</li> <li>We have learned to/that</li> <li>determine if a given number from a specified set is a solution to an equation or an inequality using substitution.</li> </ul>	<ul> <li><i>Emphasize</i> the correspondences among: (1) a solution to a pair of simultaneous two-variable equations, (2) a point of intersection of the corresponding lines, and (3) the real-world context for which the equations were created.</li> <li><i>Limit</i> the amount of required student practice in solving systems algebraically.</li> </ul>
<ul> <li>We are learning to/that</li> <li>solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs</li> <li>points of intersection satisfy both equations simultaneously</li> <li>solve systems of two linear equations in two variables algebraically</li> </ul>		

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<ul> <li>estimate solutions of two linear equations in two variables by graphing the equations</li> <li>determine the number of solutions a system of two linear equations will have based upon inspection</li> <li>solve a system of two linear equations modeling real-world and mathematical problems</li> </ul>		



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<ul> <li>8.F.A.1 Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.</li> <li>We are learning to/that</li> <li>a function is a rule that assigns to each input exactly one output</li> <li>the graph of a function is the set of ordered pairs consisting of an input and the corresponding output</li> </ul>	<ul> <li>5.OA.B.3 Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. <i>For example</i>, given the rule "Add 3" and the starting number 0, and given the rule "Add 6" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.</li> <li>We have learned to/that</li> <li>form ordered pairs consisting of corresponding terms from the two patterns and graph the ordered pairs on a coordinate plane</li> </ul>	For curricula and lessons that are well aligned to the domain of Functions as detailed in the clusters and standards within the domain, <i>no special considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.
■ 8.F.A.2 Compare properties (e.g. rate of change, intercepts, domain and range) of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). <i>For example</i> , given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change.	n/a	For curricula and lessons that are well aligned to the domain of Functions as detailed in the clusters and standards within the domain, <i>no special considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.

## **Domain: Functions**

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<ul> <li>We are learning to/that</li> <li>compare properties such as rate of change, intercepts, domain and range of two functions each represented in a different way</li> <li>8.F.A.3 Interpret the equation y = mx + b as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. <i>For example</i>, the function A = s<sup>2</sup> giving the area of a square as a function of its side length is not linear because its graph contains the points (1,1), (2,4) and (3,9), which are not on a straight line.</li> <li>We are learning to/that</li> <li>the equation y = mx + b defines a linear function</li> <li>interpret a set of points forming a straight line as the graph of a linear function</li> <li>graph linear equations</li> <li>give examples of nonlinear functions</li> </ul>	<ul> <li>6.EE.C.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. <i>For example</i>, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time.</li> <li>We have learned to/that</li> <li>two quantities which change in relationship to one another are expressed as independent and dependent variables</li> <li>write an equation using two quantities, an independent and a dependent variable, to represent a real-world problem</li> </ul>	For curricula and lessons that are well aligned to the domain of Functions as detailed in the clusters and standards within the domain, <i>no special considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.F.B.4 Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (<i>x</i>, <i>y</i>) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.</li> <li>We are learning to/that</li> <li>construct a function to model a linear relationship between two quantities</li> <li>determine the rate of change and initial value of a function from a description of a relationship or from two (<i>x</i>, <i>y</i>) values, including reading these from a table or from a graph</li> <li>interpret the rate of change and initial value of a function from a description of a relationship or from two (<i>x</i>, <i>y</i>) values, including reading these from a table or from a graph</li> </ul>	<ul> <li>7.RP.A.2 Recognize and represent proportional relationships between quantities.</li> <li>b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.</li> <li>We have learned to/that</li> <li>identify the constant of proportionality (unit rate) in equations and verbal descriptions of proportional relationships.</li> <li>identify the constant of proportionality (unit rate) in equations and verbal descriptions of proportional relationships.</li> <li>identify the constant of proportionality (unit rate) in tables, graphs, and diagrams.</li> <li>6.EE.C.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. <i>For example,</i> in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation <i>d</i> = 65<i>t</i> to represent the relationship between distance and time.</li> </ul>	For curricula and lessons that are well aligned to the domain of Functions as detailed in the clusters and standards within the domain, <i>no special considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced.

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
	<ul> <li>We have learned to/that</li> <li>two quantities which change in relationship to one another are expressed as independent and dependent variables</li> <li>write an equation using two quantities, an independent and a dependent variable, to represent a real-world problem</li> </ul>	
■ 8.F.B.5 Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally.	n/a	For curricula and lessons that are well aligned to the domain of Functions as detailed in the clusters and standards within the domain, <i>no special considerations</i> for shifting how time is dedicated are recommended. Time spent on instruction and practice
<ul> <li>We are learning to/that</li> <li>describe qualitatively the functional relationships between two quantities by analyzing a graph</li> <li>sketch a graph that exhibits the qualitative features of a function given a verbal description</li> </ul>		should <b>not</b> be reduced.

## Grade 8: New Jersey Student Learning Standards for Mathematics - Prerequisite Standards and Learning Objectives

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.G.A.1 Verify experimentally the properties of rotations, reflections, and translations:</li> <li>a. Lines are transformed to lines, and line segments to line segments of the same length.</li> <li>b. Angles are transformed to angles of the same measure.</li> <li>c. Parallel lines are transformed to parallel lines.</li> <li>We are learning to/that</li> </ul>	n/a	<ul> <li><i>Combine</i> lessons to address key concepts in congruence and <i>combine</i> lessons to address key concepts in similarity of two-dimensional figures in order to <i>reduce</i> the amount of time on this topic.</li> <li><b>Note</b>: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>
<ul> <li>verify that when a reflection, rotation, and/or translation is performed, lines are transformed to lines, and line segments to line segments of the same length</li> <li>verify that when a reflection, rotation, and/or translation is performed, angles are transformed to angles of the same measure</li> <li>verify that when a reflection, rotation, and/or translation is performed, parallel lines are transformed to parallel lines</li> </ul>		

**Domain: Geometry** 

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.G.A.2 Understand that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.</li> <li>We are learning to/that</li> <li>two figures are congruent if one can be obtained from the other by a sequence of rotations, reflections, and/or translations</li> <li>describe a sequence of transformations that maps one congruent figure onto another</li> </ul>	n/a	<ul> <li><i>Combine</i> lessons to address key concepts in congruence and <i>combine</i> lessons to address key concepts in similarity of two-dimensional figures in order to <i>reduce</i> the amount of time on this topic.</li> <li><b>Note</b>: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>
<ul> <li>8.G.A.3 Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.</li> <li>We are learning to/that</li> <li>dilate, translate, rotate, and reflect two-dimensional figures on a coordinate plane</li> <li>describe the effects of dilations, translations, rotations, and reflections using coordinates</li> </ul>	<ul> <li>6.G.A.3 Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.</li> <li>We have learned to/that</li> <li>draw polygons in the coordinate plane given coordinates of the vertices</li> <li>find the length of a side of a polygon using coordinates with the same first coordinate or the same second coordinate</li> </ul>	<ul> <li><i>Combine</i> lessons to address key concepts in congruence and <i>combine</i> lessons to address key concepts in similarity of two-dimensional figures in order to <i>reduce</i> the amount of time on this topic.</li> <li><b>Note</b>: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>8.G A.4 Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them.</li> <li>We are learning to/that</li> <li>two figures are similar if one can be obtained from the other by a sequence of dilations and rotations, reflections, and/or translations</li> <li>describe a sequence of transformations that maps one similar figure onto another</li> </ul>	n/a	<ul> <li><i>Combine</i> lessons to address key concepts in congruence and <i>combine</i> lessons to address key concepts in similarity of two-dimensional figures in order to <i>reduce</i> the amount of time on this topic.</li> <li><b>Note</b>: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>
<ul> <li>8.G.A.5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. <i>For example</i>, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so.</li> <li>We are learning to/that</li> <li>the sum of the interior angles of a triangle is 180 degrees</li> </ul>	n/a	<ul> <li><i>Combine</i> lessons to address key concepts in congruence and <i>combine</i> lessons to address key concepts in similarity of two-dimensional figures in order to <i>reduce</i> the amount of time on this topic.</li> <li><b>Note</b>: While these standards or clusters are Major Work of the Grade, during the 2020-21 school year, it is recommended that they receive lighter treatment.</li> </ul>

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<ul> <li>the measure of an exterior angle of a triangle is equal to the sum of the two remote interior angles</li> <li>when parallel lines are cut by a transversal, corresponding, alternate interior, and alternate exterior angles are congruent</li> <li>if two sets of corresponding angles in two triangles are congruent, then the triangles are similar</li> <li>use facts about angles to construct an informal argument</li> <li>8.G.B 6 Explain a proof of the Pythagorean Theorem and its converse.</li> <li>We are learning to/that</li> <li>the Pythagorean Theorem states that the square of the hypotenuse of a right triangle is equal to the sum of the squares of the other two sides</li> <li>explain a proof of the Pythagorean Theorem</li> <li>explain a proof of the converse of the Pythagorean Theorem</li> </ul>	<ul> <li>7.G.B.6 Solve real-world and mathematical problems involving area, volume and surface area of two and three- dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.</li> <li>We have learned to/that</li> <li>solve real-world and mathematical problems involving area of two- dimensional objects composed of triangles and quadrilaterals</li> </ul>	Limit lessons and problems that require students to develop and/or explain a proof of the Pythagorean Theorem. Lessons should present a proof of the theorem to students. Limit lessons about the converse of the Pythagorean Theorem.
■ 8.G.B.7 Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions.	n/a	For curricula and lessons that are well aligned to applying the Pythagorean Theorem to solve real world and mathematical problems as detailed by 8.G.B.7, <i>no special considerations</i> for

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<ul> <li>We are learning to/that</li> <li>apply the Pythagorean Theorem to determine unknown side lengths in right triangles in two-dimensional figures</li> <li>apply the Pythagorean Theorem to determine unknown side lengths in right triangles in three-dimensional figures</li> <li>apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world problems</li> <li>8.G.B.8 Apply the Pythagorean Theorem to find the distance between two points in a coordinate system.</li> <li>We are learning to/that</li> <li>apply the Pythagorean Theorem to find the distance between two points in a coordinate system.</li> </ul>	<ul> <li>6.G.A.3 Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.</li> <li>We have learned to/that</li> <li>find the length of a side of a polygon using coordinates with the same first coordinate or the same second coordinates with the same first coordinate or the same second coordinates with the same first coordinate or the same second coordinate.</li> </ul>	shifting how time is dedicated are recommended. Time spent on instruction and practice should <b>not</b> be reduced. <i>Limit</i> lessons and problems dedicated to applying the Pythagorean Theorem to find the distance between two points in a coordinate system.
• <b>8.G.C.9</b> Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems	n/a	<i>Combine</i> lessons to address key concepts with volume, with an emphasis on cylinders, in order to reduce the amount of time on this topic.

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	Instructional Considerations <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
We are learning to/that		
<ul> <li>apply the formulas for volume of a cone, cylinder, or sphere in a real-world context</li> <li>calculate the volume of a cone, cylinder, or sphere</li> <li>find a missing dimension of a cone, cylinder or sphere given its volume</li> </ul>		



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<ul> <li>8.SP.A.1 Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association.</li> <li>We are learning to/that</li> <li>construct scatter plots</li> <li>interpret scatter plots to investigate patterns of association between two quantities</li> <li>describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association</li> </ul>	<ul> <li>6.SP.B.5 Summarize numerical data sets in relation to their context, such as by:         <ul> <li>a. Reporting the number of observations.</li> <li>b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>We have learned to/that</li> <li>summarize numerical data sets in relation to their context, such as by reporting the number of observations and describing how it was measured and the units for the measurement</li> <li>describe overall patterns and any striking deviations from a data set by giving the measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation) with reference to the context such as by reporting the measures of center (median and/or mean) and variability (interquartile range and/or mean) and variability (interquartile range and/or mean absolute deviation) with reference to the context with which the data was collected</li> </ul> </li> </ul>	<ul> <li><i>Emphasize</i> using linear functions to model association in bivariate measurement data that suggest a linear association, using functions to answer questions about the data (8.SP.A.3).</li> <li><i>Combine</i> lessons for 8.SP.A.1, 8.SP.A.2 and 8.SP.A.4 to address key statistical concepts in order to reduce the amount of time on this topic.</li> <li><i>Limit</i> the amount of required student practice.</li> </ul>

#### **Domain: Statistics and Probability**

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
	<b>6.NS.C.6</b> Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.	
	c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.	
	We have learned to/that	
	<ul> <li>find and plot pairs of integers and other rational numbers on the coordinate plane</li> </ul>	
<ul> <li>8.SP.A.2 Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit (e.g. line of best fit) by judging the closeness of the data points to the line.</li> <li>We are learning to/that</li> <li>straight lines are used to model</li> </ul>	n/a	<i>Emphasize</i> using linear functions to model association in bivariate measurement data that suggest a linear association, using functions to answer questions about the data (8.SP.A.3). <i>Combine</i> lessons for 8.SP.A.1, 8.SP.A.2 and 8.SP.A.4 to address key statistical concepts in order to reduce the amount of time on this topic.
<ul> <li>straight lines are used to model relationships between two quantitative variables</li> <li>informally fit a straight line for scatter plots that suggest a linear association</li> </ul>		<i>Limit</i> the amount of required student practice.

Standard and Student Learning Objectives	Previous Grade(s) Standards and Student Learning Objectives	<b>Instructional Considerations</b> <u>SAP</u> recommendation to preserve or reduce time in 20-21 as compared to a typical year
<ul> <li>informally assess the fit of the line for a scatter plot by judging the closeness of the data points to the line</li> </ul>		
<ul> <li>8.SP.A.3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height.</li> <li>We are learning to/that</li> <li>interpret the slope and intercept in the context of bivariate measurement data using the equation of a linear model</li> </ul>	n/a	<ul> <li><i>Emphasize</i> using linear functions to model association in bivariate measurement data that suggest a linear association, using functions to answer questions about the data (8.SP.A.3).</li> <li><i>Combine</i> lessons for 8.SP.A.1, 8.SP.A.2 and 8.SP.A.4 to address key statistical concepts in order to reduce the amount of time on this topic.</li> <li><i>Limit</i> the amount of required student practice.</li> </ul>
<ul> <li>8.SP.A.4 Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. For example, collect data from students in your class on whether or not they have a curfew on school</li> </ul>	n/a	<ul> <li><i>Emphasize</i> using linear functions to model association in bivariate measurement data that suggest a linear association, using functions to answer questions about the data (8.SP.A.3).</li> <li><i>Combine</i> lessons for 8.SP.A.1, 8.SP.A.2 and 8.SP.A.4 to address key statistical concepts in order to reduce the amount of time on this topic.</li> </ul>

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<ul> <li>nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?</li> <li>We are learning to/that</li> <li>two-way tables can be used to show patterns of association in categorical data</li> <li>construct a two-way table summarizing data on two categorical variables collected from the same subjects</li> <li>interpret a two-way table by identifying joint frequencies and calculating marginal frequencies</li> <li>use relative frequencies calculated for rows or columns to describe possible association between the two variables</li> </ul>		<i>Limit</i> the amount of required student practice.

